

Mar 8, 2005

 Name

Directions: Only write on one side of each page.

I. Do any (5) of the following

1. Prove the “Opposite Side Lemma”: Given $A * B * C$ and l any line other than \overleftrightarrow{AB} meeting line \overleftrightarrow{AB} at point B . Then points A and C are on opposite sides of line l .
2. Let M be a projective plane and let M' be the interpretation of the point, line, and incident where the points of M' are interpreted to be the lines of M , the lines of M' are interpreted to be the points of M , and a point and line of M' are incident if and only if the corresponding line and point of M are incident.

Do **one** (1) of the following.

- (a) Prove that Incident Axiom 3 “makes sense” in M' .
 - (b) Prove that each line of M' is incident with at least three points of M' .
3. Using any previous results, prove Proposition 3.18.
If in $\triangle ABC$ we have $\angle B \cong \angle C$, then $AB \cong AC$ and $\triangle ABC$ is isosceles.
 4. Justify each step in the following proof of Proposition 3.17 (ASA).
Proposition 3.17 says: Given $\triangle ABC$ and $\triangle DEF$ with $\angle A \cong \angle D$, $\angle C \cong \angle F$, and $AC \cong DF$. Then $\triangle ABC \cong \triangle DEF$.
 - (a) There is a unique point B' on ray \overrightarrow{DE} such that $DB' \cong AB$.
 - (b) $\triangle ABC \cong \triangle DB'F$.
 - (c) Hence, $\angle DFB' \cong \angle C$.
 - (d) This implies $\overrightarrow{FE} = \overrightarrow{FB'}$.
 - (e) In that case, $B' = E$.
 - (f) Hence, $\triangle ABC \cong \triangle DEF$.
 5. Using any results up to and including Proposition 3.7, prove the first part of Proposition 3.8.
If D is in the interior of $\angle CAB$ then so is every other point of ray \overrightarrow{AD} except A .
 6. Do **one** (1) of the following that was not a homework problem assigned to you.
 - (a) Using any results up to and including Proposition 3.9 prove the following.
No line can be contained in a triangle.
 - (b) Using any results (on the handout sheet of propositions) up to and including Proposition 3.13 (3), prove Proposition 3.13 (4).
 - i. If $AB < CD$ and $CD < EF$, then $AB < EF$. [Note: Propositions 3.13 (c), and 3.13 (d) in the textbook are numbered 3.13 (3) and 3.13 (4) in the handout sheet.]